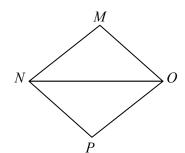
Tutor-USA.com Worksheet Geometry

Triangle Congruence Proofs – SSS, SAS

Name: ______
Date: _____

Given: $\overline{MN} \cong \overline{PO}$ and $\overline{MO} \cong \overline{PN}$

Prove: $\triangle MNO \cong \triangle PON$



Proof:

$$\overline{MN} \cong \overline{PO}$$

Given

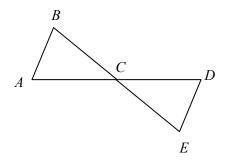
$$\overline{MO}\cong \overline{PN}$$

Given

$$\overline{NO} \cong \overline{ON}$$

 $\Delta MNO \cong \Delta PON$

2) $\overline{AC} \cong \overline{DC}$ and $\overline{BC} \cong \overline{CE}$. Write a paragraph proof to show that $\triangle ABC \cong \triangle DEC$

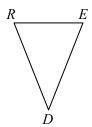


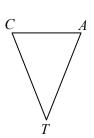
Given: $\overline{AB} \cong \overline{CB}, \overline{AD} \cong \overline{CD}$

Prove: $\triangle ABD \cong \triangle CBD$

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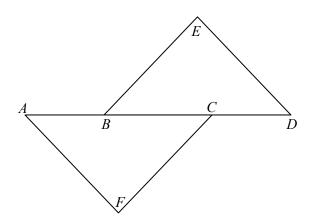
4) Given: $\overline{RE} \cong \overline{CA}$, $\overline{RD} \cong \overline{CT}$, $\angle R \cong \angle T$ Prove: $\Delta RED \cong \Delta CAT$





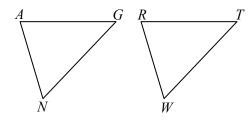
Given: $\overline{AB} \cong \overline{CD}$, $\overline{AF} \cong \overline{DE}$, $\angle A \cong \angle D$

Prove: $\Delta FAC \cong \Delta EDB$

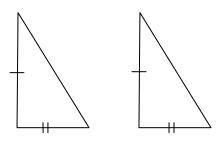


Decide whether you can use SSS or SAS Postulate to prove that the triangles below are congruent. If so a) write the congruence statement and b) identify the postulate. If not, write not possible.

6) Given: $\overline{AN} \cong \overline{RW}$, $\overline{GN} \cong \overline{TW}$, $\angle N \cong \angle W$



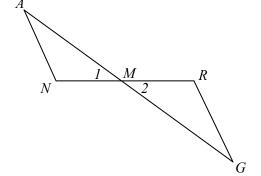
7)



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Supply the reasons for the proof below.

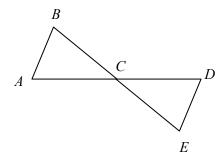
8) Given: M is the midpoint \overline{AG} and of \overline{NR} Prove: $\Delta ANM \cong \Delta GRM$



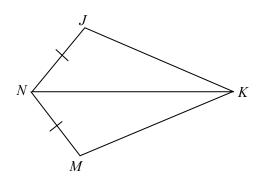
- 1. ∠1 ≅ ∠2
- 2. M is the midpoint of \overline{AG}
- 3. $\overline{AM} \cong \overline{GM}$
- 4. M is the midpoint of \overline{NR}
- 5. $\overline{NM} \cong \overline{RM}$
- 6. $\triangle ANM \cong \triangle GRM$

Write a two Column Proof.

9) Given: \overline{AE} and \overline{BD} bisect each other Prove: $\Delta ACB \cong \Delta ECD$



10) Given: \overline{NK} bisects $\angle JNM$, $\overline{NJ} \cong \overline{NM}$ Prove: $\Delta NJK \cong \Delta NMK$



Answer Key

- 1) Reflexive Property of Congruence, SSS
- 2) $\angle ACB \cong \angle DCE$ because they are vertical angles. $\triangle ABC \cong \triangle DEC$ by SAS

$$\overline{AB} \cong \overline{CB}$$
 Given

$$\overline{AD} \cong \overline{CD}$$
 Given

$$\overline{BD} \cong \overline{BD}$$
 Reflexive

$$\triangle ABD \cong \triangle CBD$$
 SSS

4) Not enough information. Angle t is not included between the congruent sides. Triangles may or may not be congruent.

$$\overline{AF} \cong \overline{DE}$$
, Given; $\angle A \cong \angle D$, Given; $\overline{AB} \cong \overline{CD}$, Given

- AB = CD, def. congruent segments; AB + BC = CD + BC, Addition Prop. of Equality
- 5) AC = BD, Segment Addition Postulate; $\overline{AC} \cong \overline{BD}$ def. of congruent segments $\Delta FAC \cong \Delta EDB$ SAS

6) a.
$$\triangle ANG \cong \triangle RWT$$
 b. SAS

- 7) Not enough information
- 8) 1) Vertical Angles, 2) Given, 3) Def. of midpoint, 4) Given, 5) Def. of midpoint, 6) SAS

$$\overline{AE} \& \overline{BD}$$
 bisect each other, Given

$$\overline{AC} \cong \overline{EC}$$
, Def. Segment Bisector

$$\overline{BC} \cong \overline{DC}$$
, Def. Segment Bisector

$$\angle ACB \cong \angle ECD$$
, Vertical Angles are congruent

$$\Delta ACB \cong \Delta ECD$$
 SAS

$$\overline{NK}$$
 bisects $\angle JNM$, Given

$$\angle JNK \cong \angle MNK$$
, Def. Angle Bisector

$$\overline{NJ} \cong \overline{NM}$$
, Given

$$\overline{NK} \cong \overline{NK}$$
, Reflexive

$$\Delta NJK \cong \Delta NMK$$
, SAS